



UNIVERSITÀ DEGLI STUDI DI SALERNO

Department of Industrial Engineering
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Analysis of condensation phenomena in fiber-based cup

Thesis in
Transport Phenomena

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Alla Donna che mi ha insegnato tanto.
E a Me stessa.

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Abstract

The growing reduction in the production and use of plastics has brought about new challenges in the packaging industry, pushing research toward more innovative and sustainable solutions. Among these alternatives, paper cups have emerged as a promising choice. However, they present unique challenges, primarily due to their hygroscopic properties. These materials tend to absorb moisture from the surrounding environment, which can lead to a decrease in their structural integrity when used to contain cold liquids. In such scenarios, condensation forms on the outer surface of the cup, and unlike plastic, this moisture permeates into the paper, altering its physical properties.

The goal of this study was to develop and validate a model capable of accurately describing the condensation and moisture transport phenomena within a paper cup. To begin, the key variables and functions of the system were identified and formalized into equations. These equations were then simulated using COMSOL Multiphysics software, which allowed for a precise and detailed representation of the physical processes involved. The model's validity was further ensured by comparing its predictions with experimental data, including temperature, humidity, and water content measurements collected during the experiments.

Through this research, it was concluded that the transport phenomena and vapor condensation within the pores of the paper cup are closely linked to external environmental conditions. Specifically, as external temperature and relative humidity increase, the driving force for condensation becomes stronger. When the temperature of the surroundings approaches that of the liquid inside the cup, and the

material contains a certain amount of water vapor under favourable conditions, condensation begins to occur within the material itself.

It is important to emphasize that even when the liquid diffusivity is not considered, a portion of the vapor inside the material still condenses, albeit in minimal amounts. The primary driving force is generated by the liquid penetrating the material, but it is essential to also account for the fraction of vapor that condenses and is already in equilibrium within the material.

Therefore, it is essential to consider not only the external condensation on the surface of the cup but also the internal condensation of water vapor that occurs within the material. This internal condensation plays a crucial role in the overall moisture dynamics and contributes to the material's performance and durability.

In summary, this study highlights the importance of understanding the interaction between the material and the surrounding environment. It emphasizes that both external and internal condensation mechanisms must be considered to fully grasp the moisture transport and condensation behavior in paper cups. Future research could focus on refining the model to better predict these phenomena under varying environmental conditions and further optimize the material properties for improved performance.

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